

Partial squeeze film levitation modulates fingertip friction

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When touched, a glass plate excited with ultrasonic transverse waves feels notably more slippery than it does at rest. To study this phenomenon, we use frustrated total internal reflection to image the asperities of the skin that are in intimate contact with a glass plate. We observed that the load at the interface is shared between the elastic compression of the asperities of the skin and a squeeze film of air. Stroboscopic investigation reveals that the time evolution of the interfacial gap is partially out of phase with the plate vibration. Taken together, these results suggest that the skin bounces against the vibrating plate but that the bounces are cushioned by a squeeze film of air that does not have time to escape the interfacial separation. This behavior results in dynamic levitation, in which the average number of asperities in intimate contact is reduced, thereby reducing friction. This improved understanding of the physics of friction reduction provides key guidelines for designing interfaces that can dynamically modulate friction with soft materials and biological tissues, such as human fingertips.

acoustic | squeeze film | biotribology | roughness | haptics

Holding a glass of wine, searching for keys in one's pockets, and assessing the quality of fabric are everyday tasks that involve precise and unambiguous perception of the friction between the skin and the environment. The somatosensory and motor control systems integrate multiple neural signals to determine the state of adhesion of the surface in contact with the skin, thus enabling perception (1–3) and in the context of grasp, ensuring that slippage is under control (4–6). Considering the central role of fingertip–surface friction in both manipulation and tactile perception, it is not surprising that many technologies attempt to control this effect to produce artificial and programmable tactile sensations (7–9). The use of transverse ultrasonic vibrations to reduce tactile friction (10) has proven to be a strong candidate for surface haptic displays that might be integrated with the ubiquitous touchscreen interface (11–13). A typical architecture consists of a glass plate—which may be placed in front of a graphical display—with piezoelectric actuators glued along one edge and used to excite a $0 \times n$ flexural resonance. The resonant frequency may be ~ 30 kHz and the peak to peak vibration amplitude may be up to $5 \mu\text{m}$ at the antinodes. A finger placed on the plate experiences markedly reduced friction as the vibration amplitude is increased as shown in [Movie S1](#).

A full understanding of the physical principle behind friction reduction has proven elusive. Two leading hypotheses have been put forward. The first hypothesis stems from an application of Reynolds' lubrication theory to the thin film of air between the fingertip and vibrating plate. The vibrations lead to time-averaged compression of the air, thereby creating an overpressure that levitates the skin. The second hypothesis postulates that the skin does not stay in close contact with the surface but instead, bounces off of it, leading to shorter time in contact and therefore, a time-averaged reduction in friction.

We present evidence that the friction reduction effect cannot be fully explained by either of these theories. We argue that friction reduction is the result of a load sharing between compressed air and those asperities on the skin that are in intimate

surface contact. Other recent evidence shows that the dynamics of the skin (in particular, its viscoelastic properties) is key to friction reduction (14). Combined with our evidence, the picture that emerges is of friction reduction by bouncing but bouncing off of compressed air as well as the surface.

Background

The roughness of the skin is often modeled as a random height profile following a normal distribution (15). When in contact with a plate, at rest or in motion, the contact area with the skin is formed by deformation of the highest peaks (asperities) when they come into intimate contact with the counterbody. This area, called the true area of contact, is often several orders of magnitude smaller than the apparent contact area seen at a macroscopic scale. Various models have been used to estimate the value of the true area as a function of the applied force. Greenwood and Williamson (16) treated asperities as spheres of constant radius and random heights. Bush et al. (17) went further to treat both the surface profile and the gradients as correlated random processes. In both papers, Hertzian contact mechanics were used to derive a relation between force and contact area (16, 17). More recently, Persson (18) has used a self-similar fractal model of the surface profile to derive the relation between the interfacial separation—the average gap between both surfaces—and the external load. Interestingly, all of these theories converge to the same relationship for small loads, wherein the true area of contact is proportional to the negative exponential of interfacial separation.

The true area of contact has a central role in friction. Each asperity making intimate contact can support an adhesive shear load proportional to its contact area. The friction force experienced by the finger is the sum of the shear loads on the contacting asperities (19). Because friction force is proportional to

Significance

Touchscreens have redefined human–computer interfaces. Although flexibility in the design of interfaces has dramatically increased, users are still confronted with a flat, featureless glass plate that cannot provide any tactile cues. Exciting this plate with ultrasonic waves reduces the friction experienced by a user's finger, enabling tactile feedback directly on the surface. For vibration amplitudes of $\pm 3 \mu\text{m}$, we measured a reduction of up to 95% in the friction force experienced by a sliding finger. Using special illumination techniques and microscope imaging, we show that this reduction of friction is because of the skin bouncing on a layer of air trapped between the plate and the surface of the finger.

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true area of contact, which itself is proportional to load, according to multiscale theory of contact (15), we can appreciate the basis for Amontons's first and second laws that state that friction is proportional to normal load and independent of the macroscopic apparent area. The value of the interfacial shear stress for the skin of fingertips on glass usually is found to be ~ 4.8 kPa (20, 21). Measurement of the true area of contact by acoustical and optical methods supports this adhesive view of friction (22–24). Moisture significantly affects tactile friction by softening the stratum corneum, enabling it to conform better to the surface, which greatly increases the true area of contact (15, 25–27). In this study, moisture is likely responsible for much of the variability in friction force measurements. When a fingertip is pressed against a very flat surface, such as glass, the sweat glands are occluded, and moisture builds up rapidly. We also developed an artificial finger, enabling us to explore the mechanics of friction reduction without suffering from the measurement variability introduced by moisture.

Because all models of fingertip friction lead to the conclusion that friction is proportional to the true area of contact, we ask if this is also true in the case of ultrasonic friction reduction? Also, if this statement is true, by what mechanism does vibration reduce the time-averaged area of contact? In seeking answers, one consideration must be the role of air. It is well-known that acoustic waves in air create a radiation pressure when reflecting off an object (28). For smooth planar objects, stable levitation can occur when the acoustic radiation pressure balances the weight (29, 30). For levitation distances significantly smaller than the wavelength of sound (i.e., by at least three orders of magnitude), the behavior becomes dominated by the elasticity and viscosity of the fluid trapped between the actuator and the reflector surface (31, 32). This trapped fluid is known as a squeeze film. In this scenario, which is typical of tactile friction reduction devices, a squeeze film levitation model may be derived from the Reynolds' lubrication equation to compute the levitation force (33–35). This model depends on a nondimensional "squeeze number" that is, essentially, a ratio of the time required to squeeze air out of the gap to the period of oscillation. For large-enough squeeze numbers, the air may be considered to be completely trapped, and the pressure may be shown to be $5/2 p_0 \alpha^2/u^2$, where p_0 is atmospheric pressure, α is the amplitude of motion, and u is the squeeze film thickness. Acoustic levitation does not on its own, however, explain the progressive reduction of friction with increasing vibration amplitude that is observed in tactile interfaces. Watanabe and Fukui (10) proposed that the load is shared between points in intimate contact and the overpressured film of air and presented a simple model. Their predictions, however, do not match the amplitude

dependence that we present here, and they do not provide experimental validation (10).

In this study, the contact area between a human fingertip and a vibrating glass plate was imaged by frustrated total internal reflection. This technique provides a detailed picture of the spatiotemporal behavior of the contact area, which is shown to be consistent with predictions stemming from a combination of squeeze film theory and an exponential contact model. Fig. 1 illustrates the balance of forces proposed in this research.

Results and Discussion

Each participant placed his or her finger on a glass plate that was driven side to side by a servomechanism for the purpose of measuring friction, and it experienced various amplitudes of ultrasonic vibration. The tribometric measurements confirmed that the friction force resisting the lateral motion consistently decreased as the amplitude of the out of plane oscillation increased. The reduction of friction reached 70% to 98%, with an average across participants of 90% at an amplitude of $3 \mu\text{m}$ and a frequency of 29 kHz. A schematic of the apparatus is shown in Fig. 2A and construction details are presented in *SI Materials and Methods*. No correlation with age or moisture of the skin could be established. The relation between amplitude and friction force is monotonic, and in some cases, a plateau is observed at low amplitude. For large-enough amplitudes, the curve flattens as it approaches near-frictionless contact, as seen in Fig. 2B. The relationship between friction force and amplitude of vibration for each participant is compared with the model in Fig. S1.

The contact imaging scheme used here leverages frustrated total internal reflection, which illuminates only those asperities that are within a few hundred nanometers of the glass plate, thus producing highly contrasted images of the area of contact. Each pixel of the image receives an amount of light that is proportional to the sum of the area made by every single asperity in intimate contact and thus, offers an estimation of the local true area of contact. A typical recording is shown in *Movie S2*. Simultaneous measurement of kinetic friction force and imaging of the scattered light from the skin reveals a remarkable correlation between the overall brightness of contact and the instantaneous friction force while sliding. A linear relationship was found between total brightness and friction force, with coefficients of determination $r^2 = 0.83$ – 0.96 for the human subjects and $r^2 = 0.88$ for the artificial finger. The error can be explained by the diffusivity of the skin and surroundings as well as force sensor noise. Data and regressions are given in Fig. 2C. This correlation is well in line with the adhesive theory of friction discussed above. The ratio between brightness and force remains within a 30% margin across participants. The variation is likely caused by differences in reflectance of the skin as well as the presence of moisture and

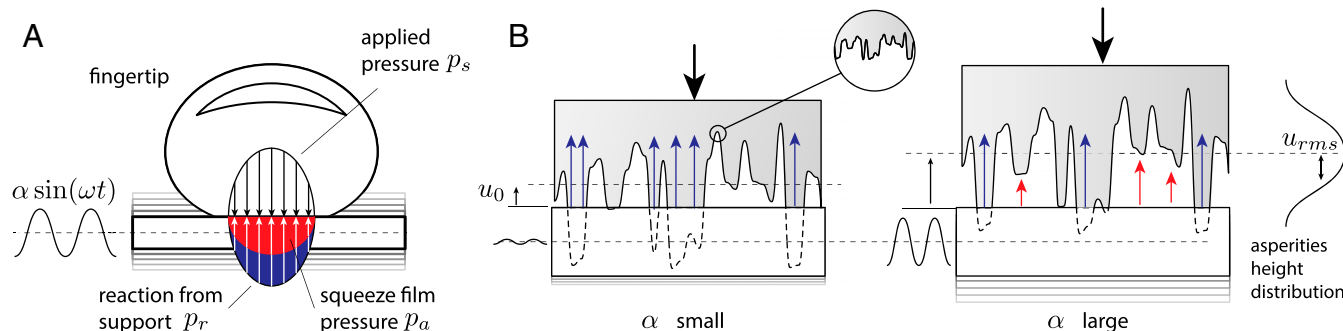


Fig. 1. (A) Balance of time-averaged pressure when the plate undergoes ultrasonic vibrations. (B) View of the asperities. At low amplitude, the reaction from the support balances the pressing force completely. At high amplitude, both the reaction from the support and the squeeze film pressure contribute to balancing the pressing force. In addition, the average interfacial separation is increased.

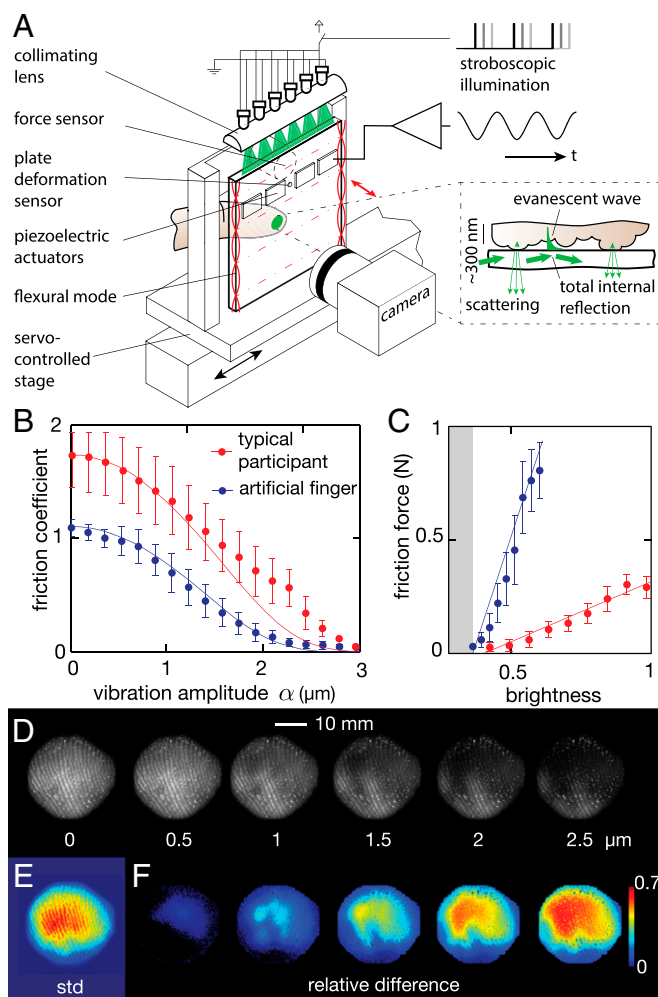


Fig. 2. (A) Experimental setup. The vibrating plate is mounted on a servo-controlled stage equipped with a six-axis force sensor. Illumination from the side of the plate provides a uniform illumination of the true contact area through frustrated total internal reflection (A, *Inset*). (B) The sliding friction force gradually decreases with increasing vibration amplitude. The line represents the (C) brightness and friction force correlation. The illumination technique reveals those asperities that are within a few hundred nanometers of the plate; therefore, the spatial average of the brightness received by the camera is linearly correlated with the friction force and under the adhesive theory of friction, linearly correlated with the true area of contact. (D) Images of the contact area under ultrasonic vibration amplitudes of 0–2.5 μm . (E) Spatial distribution of the variation of brightness over a cycle where the amplitude of stimulation is slowly varying. The center of the contact experiences the most variation, whereas the edge remains unaffected. (F) The difference between the brightness at selected amplitudes and the brightness at rest highlight those areas that are more or less affected by vibration.

the dynamics of friction. [Movie S3](#) illustrates that the contact area fluctuates during steady-state sliding and exhibits dynamics after a rapid change in vibration amplitude. These effects explain some of the variation in friction force measurement. Because of a different reflectance, the artificial finger has a ratio of brightness to force eight times larger than the average human finger, but it shows the same linear correlation. The strong linear relationship seen in Fig. 2C and Fig. S2 is the basis for treating the frustrated total internal reflection measurement of contact area as a proxy for friction force. Notably, frustrated total internal reflection imaging provides data at temporal and spatial scales out of reach for standard force sensors.

The reduction of contact area with increasing vibration amplitude is an indicator that the process involves squeeze film levitation and does not solely rely on intermittent contact of the finger. In fact, if a squeeze film did not support some of the normal load, the brightness of the contact, averaged over thousands of cycles, would remain constant, because the average contact force would necessarily balance the applied force. Clearly, this constant brightness is not the case. Thus, air plays a critical role in reducing the true area of contact by increasing the interfacial separation.

At the scale of the entire finger pad, the measurement fits well with the theory of squeeze film levitation. As the plate oscillates, the air trapped between it and the skin cannot escape and gets compressed. This compression follows a nonlinear process that creates a net force pushing the skin away from the plate and increasing the interfacial separation between the skin and the glass. However, because the roughness of skin is almost one order of magnitude larger than the increased separation, some contacting asperities never do break contact, leading to only partial reduction of friction. The pressing force that pushes the skin toward the glass is balanced by the force from squeeze film pressure as well as the resultant force from the asperities that remain in intimate contact. Both reaction forces depend on the interfacial separation u but with different relations. The contact forces typically fall off as $\exp(-(u-u_0)/u_{rms})$, whereas the squeeze film force F_a is proportional to $\alpha^2/u^2 + O(\alpha^4)$. Because the pressing force F_p is perfectly counterbalanced by the contact force when $\alpha=0$, the equilibrium may be written as $F_p(1 - \exp(-(u-u_0)/u_{rms})) = F_a$. The full derivation is presented in [SI Results and Discussion](#) and results illustrated in Fig. S3. The comparison with measurement shows good agreement, especially in the low-amplitude regime where the acoustic force is small.

It is also instructive to look at the spatial distribution of brightness across the finger pad. The contact between the finger and the plate is roughly an ellipse shape as expected from the contact of an ellipsoid and a plane. The luminance field across this ellipse provides information about the local contact pressure, which may be calculated by multiplying the local brightness by the overall ratio of normal force to total brightness. The results show that normal pressure is maximum at the center of the ellipse and decreases toward the edges in a parabolic fashion, which is consistent with the Hertzian contact previously reported in the literature (21, 36, 37). The distribution of pressure fits $p_r = p_h \sqrt{1 - (r-r_0)^2/a^2}$, where r is the radial coordinate, r_0 is the lateral shift, and a is the radius of the apparent contact area. The goodness of fit for each participant varies between $r^2 = 0.92$ and $r^2 = 0.98$, and Hertzian pressure p_h is on the order of 2.8 ± 1.4 kPa.

The addition of plate vibrations has a distinctive effect on the contact pressure. By subtracting the brightness of the resting finger from the brightness of the contact during vibration, the overpressure caused by the squeeze film can be estimated as illustrated in Fig. 3A. For each participant, the squeeze film pressure is highest in the center of the contact area and falls off to zero toward the edges. At first glance, it could be postulated that this distribution of squeeze film pressure is caused by an edge effect: the squeeze film pressure is constrained to be atmospheric at the edge and therefore, expected to increase toward a maximum value in the center. Such a broad edge effect, however, would be associated with an unrealistically small squeeze number. Fitting the distribution of pressure derived from the lubrication theory in the works in refs. 35, 38, and 39 to the data leads to squeeze number between 1 and 30, whereas the value derived from estimates of contact area, frequency, and interfacial displacement is between 150 and 1,000. At these higher values, the edge effect should be quite minimal. Instead, a more plausible explanation arises from the observation that the nominal gap between the skin and plate is not uniform across the

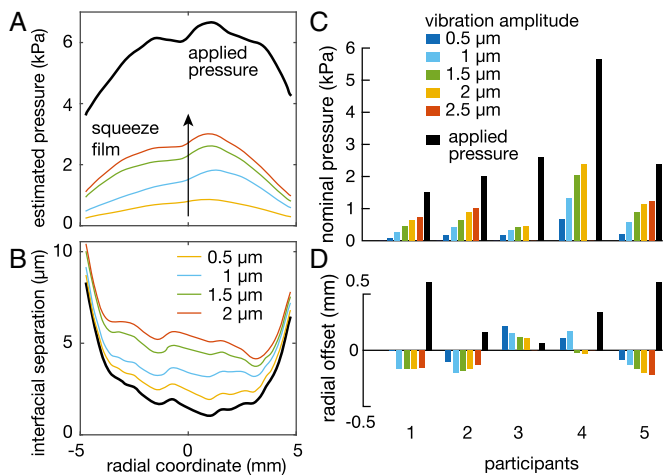


Fig. 3. (A) Local brightness corresponds to the number of asperities in contact, which depends on pressure. Brightness scaled by the normal force reveals the pressure profile along the central axis of the contact. The squeeze film pressure is highest in the center of the contact. (B) Calculated interfacial separation. Larger applied pressure in the center results in a lower gap, which in turn, influences the acoustic radiation pressure created by the squeeze film of air. (C and D) Results from the fitting procedure with a Hertz contact model. The nominal pressure and the squeeze film pressure are asymmetric.

contact because of the Hertzian pressure distribution. The applied pressure $p_s(r)$ is maximum in the center, which in turn, means that the nominal interfacial separation $u_0(r) = u_{rms} \log(p_c/p_s(r))$ is smaller at the center, producing a stronger squeeze film effect according to $1/u(r)^2$.

For convenience, the estimated acoustic pressure distribution was also fitted with a Hertzian profile, for which the goodness of fit reached $r^2 = 0.86 \pm 0.04$. Although the nominal pressure p_n increased with increasing amplitude (Fig. 3C), the lateral shift r_0 (Fig. 3D) and the estimated radius of action a remained within 10% of the average value across amplitudes. The estimated radius a of the acoustic pressure distribution was systematically smaller than the radius of the nominal contact area by an average of 0.85 ± 0.6 mm, which is likely to be because of the departure of acoustic pressure distribution from a Hertzian model. The position shift of the center of the squeeze film pressure distribution was also quite different from the normal pressure distribution. Although the normal pressure is shifted toward the proximal section of the fingertip, the squeeze pressure is, for the most part, shifted distally. This asymmetry is likely to be the result of the complex structure of the s.c. tissues and bone that have spatially dependent mechanical properties.

High-speed stroboscopy was used to image the intracycle contact area with a time resolution of $1 \mu s$, revealing that dynamic effects are at play. Fig. 4A and B illustrates the typical dependence of brightness on phase and plate displacement. Brightness of the contact is nearly sinusoidal at the plate vibration frequency, with total harmonic distortion between -10 and -8 dB for amplitudes higher than $0.5 \mu m$. Consistent with long-exposure results, the average brightness decreases as the vibration amplitude increases. However, the peak to peak variation of brightness increases significantly with increasing amplitude, from 0% to 22% of the nominal brightness. [Movie S4](#) depicts a representative sample of the brightness variations on a microsecond timescale.

Remarkably, at a fixed amplitude of vibration, the temporal variation and nominal value of brightness are in proportion for the majority of pixels in the contact image as shown in Fig. 4D. This correlation can be explained if we consider that the true area of contact is $A = A_0 \exp(-(u - u_0)/u_{rms})$, with u being the gap during levitation and u_0 being the gap at rest. The variation

of levitation height caused by the combined motion of the plate and the skin induces a change in brightness so that $\delta u = u_{rms} \delta A/A$. The ratio between fluctuation and average value of the brightness is fully derived in [SI Results and Discussion](#), and experimental values of this ratio are graphed in Fig. 4E as a function of amplitude for each participant.

It is worth noting that the data lean toward refuting the hypothesis of intermittent contact and instead, favoring the hypothesis of load sharing between a squeeze film and asperities. Indeed, the maximum brightness observed with the stroboscopic illumination consistently decreased with increasing amplitude. This observation means that the smallest interfacial separation between the vibrating glass plate and the skin increases with increasing amplitude of the plate vibrations. If intermittent contact was the main mechanism, the impact caused by the collision would create a spike of brightness greater than that seen

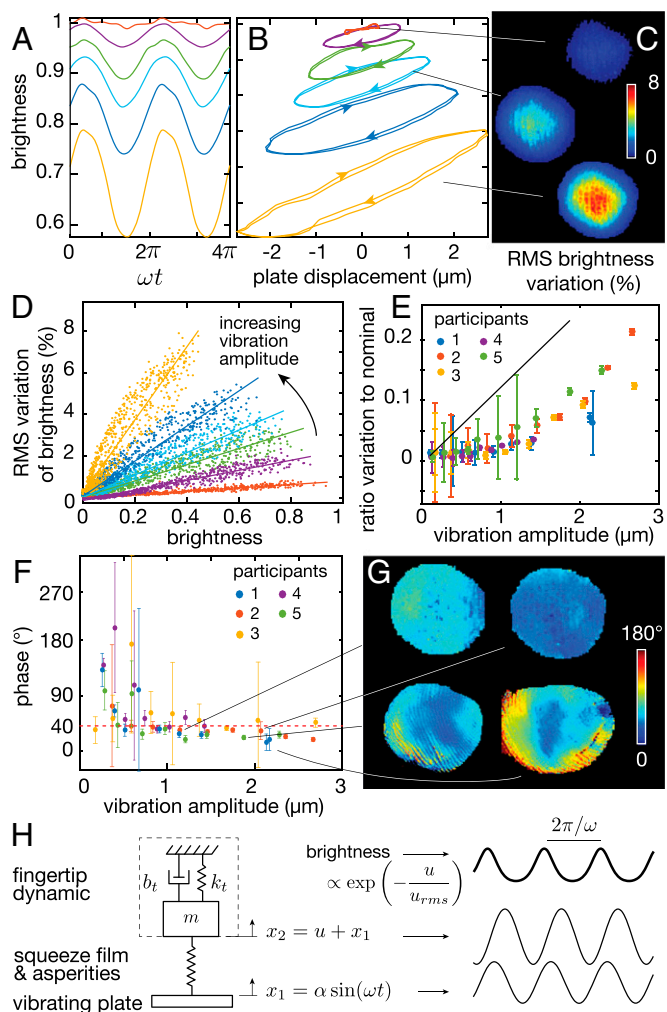


Fig. 4. (A) Time domain variation of brightness. Changes in brightness closely follow a sinusoidal pattern. (B) Phase portrait of brightness and plate position. Increased amplitude decreases the average brightness but increases the variation. (C) Selected images of the spatial distribution of brightness variation. (D) Variation and average brightness are correlated in each image. The lines are linear regressions. (E) The ratio is a function of the amplitude of stimulation. The prediction from a model with large skin roughness $u_{rms} = 5 \mu m$ is in black. (F) Phase between motion of the plate and the interfacial separation as a function of amplitude and participant. (G) Selected spatially distributed phase plots. Large variations of phase occur across trials. (H) Simplified linear model of the skin bouncing off the film of air leads to behaviors similar to the experimental observations.

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Supporting Information

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SI Materials and Methods

Friction Reduction Device. The friction reduction apparatus was built around a $67 \times 50 \times 5$ -mm³ borosilicate glass plate actuated by two piezoelectric transducers (smp131w89t10; Steminc). The plate was excited in the 3×0 normal mode, which corresponds to a standing flexural wave with 19-mm nodal spacing at a resonant frequency of $f_0 = 29,080$ Hz. A finite element analysis (Comsol Multiphysics 5.0) presented in Fig. S5A shows the modal shape of the plate. The finite element analysis reveals that the standing wave ratio is 58 with a fingertip, modeled by 20 N·s/m damper, in contact with the center of the plate. In the experiment, only the center crest was used to provide the out of plane motion necessary to reduce friction. The amplitude of the center antinode varies by only 3% of its nominal value. The real time deformation of the glass is measured by a piezoelectric disk that was calibrated with a laser Doppler vibrometer. A power amplifier (A-303; A.A. Lab System Ltd) drives the actuators over a range of ± 200 V, which translates to a maximum unloaded displacement of $\pm 3 \mu\text{m}$, constant over the entire width of the plate.

Friction Experiment. The ultrasonic plate and the illumination system were mounted on a servo-controlled stage (KR26; THK Co.) equipped with a six-axis force sensor (Nano 17; ATI Industrial Automation). The device measures normal and lateral forces while sliding the plate across the static finger at a 10-mm/s velocity. The stage was driven with a trapezoidal velocity profile to provide a constant velocity over the region of interest, avoiding the effect of the plate inertia on force measurements. The camera was placed at the other side of the plate pointed at the finger in contact with the glass. The position of the slide, forces acting on the glass, and amplitude of the vibration were measured by a 16-bit data acquisition board at a rate of 2 kHz. The data were numerically filtered by a zero-lag, four-pole Butterworth filter with a cutoff frequency 100 Hz, and then, they were down-sampled to match the timestamp provided by the camera. The resulting noise floor was 10 mN.

Imaging System and Image Processing. The experiment used frustrated total internal reflection to provide a high contrast between the regions that are in intimate contact with the glass and the background. Frustrated total internal reflection imaging is based on the coupling of the material in contact (i.e., the skin) with the electromagnetic evanescent wave present at the surface of the glass plate. For an incident electromagnetic wave of wavelength- λ reflecting at an angle with the surface- θ , the evanescent wave decays exponentially with the distance z away from the plate, such that brightness $b = \exp(-\kappa z)$, where $\kappa = 2\pi/\lambda \sqrt{n_g \sin(\theta)}$, and $n_g = 1.52$ is the relative refraction index between glass and air. In this experimental setup, the light was provided at the edge of the glass plate by 10 high-power green LEDs (XPEBGR, Cree Inc.) with a wavelength of $\lambda = 527.5 \pm 7.5$ nm focused to a $\pm 20^\circ$ narrow beam by a planoconvex lens over a 60-mm span. In the described condition, the brightness is reduced to 5% of its initial value when the objects are ≈ 300 nm apart.

To measure the time-averaged brightness of the contact, the illumination was driven by a constant current source of 1 A while the ultrasonic vibration was turned on. The skin and plate undergo a harmonic motion and reach steady state within milliseconds. High-speed imaging relies on the steady-state behavior by illuminating the contact with stroboscopic flashes that are synchronously triggered with the motion of the plate. The evolution of the contact is imaged at a reduced pace corresponding to the difference between

the frequency of the ultrasonic vibration and the frequency of the light flashes. In these experiments, the rate is reduced to 1.0 Hz. The illumination was driven with 60-V pulse signal at a frequency $f_0 + 1$ Hz, where f_0 is the frequency of the ultrasonic vibration, and width is $1 \mu\text{s}$. The dynamic light source was verified with a photodiode having a 150-MHz frequency bandwidth (PDA10A; Thorlabs Inc.). The time response of the illumination is shown in Fig. S5B. The light pulse is shorter than $1.2 \mu\text{s}$, allowing for a time resolution of 30 points per cycle of the 30-kHz ultrasonic vibration. The delay between the rising edge of the pulse and the beginning of the light pulse was $0.4 \mu\text{s}$ and accounted for during the post-processing. The images of the contact were captured by a CCD camera (v5.1; Phantom Vision Research) equipped with a macro-lens (Nikkor 105 mm; Nikon Corp.) at a rate of 50 images per second. The optical setup achieved a resolution of $18 \mu\text{m}$ per pixel.

Microsecond imaging data were filtered to remove artifacts caused by tremors. To do so, the time evolution of each pixel was transformed into the Fourier domain, multiplied with a Dirac comb with the fundamental frequency as baseline, and then, converted back into the time domain.

SI Results and Discussion

Roughness and Nominal Separation. When two elastic solids with rough surfaces are pressed together, they make contact only on a fraction of the apparent area composed by the contact of the tallest asperities. Larger normal pressures will increase the true area of contact by bringing more asperities into contact with the counterbody. The separation between the two surfaces $u(x, y)$ as a function of lateral coordinates will vary in a random fashion and usually follow a normal distribution with SD u_{rms} (Fig. 1A). Many engineering and natural surfaces are self-affine fractal surfaces, where the roughness is defined at a certain level of magnification. In the case of skin, interferometer measurements of alginate casts reveal that the Hurst exponent is close to 0.8 and that the SD, when not compressed, is close to $u_{rms} = 5 \mu\text{m}$ (15). The float borosilicate glass plate acting as a counterbody is considered perfectly rigid and smooth.

The Persson theory of contact states that the pressure from the reaction of the support is

$$p_r = p_c \exp\left(\frac{-u}{u_{rms}}\right), \quad [S1]$$

where $p_c = 0.375 q_0 u_{rms} E / (1 - \nu^2)$ is the absolute pressure coefficient that depends on the roughness and elastic properties of the material (18). In this case, $q_0 = 10^4 \text{ m}^{-1}$ is the magnification at which the rms of the height distribution is measured to be $u_{rms} = 5 \mu\text{m}$. $E = 20 \text{ MPa}$ is the Young's modulus of the stratum corneum, and $\nu = 0.5$ is its Poisson's coefficient.

At rest, without any vibration, $\alpha = 0$, the reaction from the support p_r is equal in magnitude and opposite in direction to the external pressure p_s , and the interfacial separation is denoted u_0 , which leads to an alternative expression for the Pearson pressure p_c :

$$p_c = p_s \exp\left(\frac{u_0}{u_{rms}}\right) \text{ and } u_0 = u_{rms} \ln\left(\frac{p_c}{p_s}\right). \quad [S2]$$

This function leads to the following expression for the contact force: $p_c = p_s \exp((-u + u_0)/u_{rms})$.

Levitation Forces from Squeeze Film Theory. When subjected to transverse vibrations at ultrasonic frequencies, any air trapped

between the rough surface of the skin and the plate undergoes a nonlinear compression cycle that results in a net levitation pressure. The Reynolds number under these conditions is typically in the order of $Re = 0.1$, from which we conclude that inertia forces in the fluid are small compared with viscous forces and that the flow is laminar. Acoustic levitation pressure is then derived from the Reynolds equation:

$$\frac{\partial}{\partial x} \left(\frac{\bar{u}^3 p}{12\mu} \frac{\partial p}{\partial x} \right) = \frac{\partial(p\bar{u})}{\partial t}, \quad [\text{S3}]$$

where $\bar{u} = u + \alpha \sin(\omega t)$ is the instantaneous interfacial separation. The left-hand side captures Couette flow, and the right-hand side is the variation of molecular mass (time derivative of Boyle's law). The squeeze number $\sigma = 12\omega\mu L^2 / (p_0 u^2)$ provides a non-dimensionalized measure of the ratio between the elastic behavior of the air cushion and the viscous dissipation at the edge of the contact area. In the our configuration, the size of the contact is $L \approx 10^{-2}$ m, the angular frequency is $\omega \approx 250 \cdot 10^3$ rad/s, and the gap size is $u \approx 2u_{rms}$, which leads to a squeeze number $\sigma \approx 600$.

The distribution of the squeeze pressure across the width of the contact is found to follow a uniform distribution within a 10% margin for squeeze numbers $\sigma > 150$. For such a high number, the flow that escapes on the side of the contact is almost negligible. The reader can refer to refs. 35 and 38 for detailed analyses of the distribution of pressure.

Because no flow escapes the gap, the fluid mass remains constant or $p\bar{u} = \text{cst}$. The time integral of Eq. S3 over one cycle leads to

$$\int_0^{2\pi} \frac{\partial}{\partial x} \left(\bar{u}^3 p \frac{\partial p}{\partial x} \right) dT = 0, \quad [\text{S4}]$$

with $T = \omega t$. Integrating twice over the spatial coordinate and noting that $dp/dx = 0$ in the center of the contact leads to

$$\int_0^{2\pi} \bar{u}^3 p^2 dT = C_1 \quad \forall x. \quad [\text{S5}]$$

At the edge, the pressure is atmospheric, which leads to

$$\int_0^{2\pi} \bar{u}^3 dT = \int_0^{2\pi} (u + \alpha \cos(T))^3 dT = \frac{C_1}{p_0^2} = 2\pi u \left(u^2 + \frac{3}{2\alpha^2} \right). \quad [\text{S6}]$$

The rest of the contact undergoes isothermal expansion and contraction of the air; therefore, $p\bar{u} = C_2$ or $p^2 = C_2^2 / u^2$. It follows that

$$C_2^2 \int_0^{2\pi} \bar{u} dT = 2\pi (u^2 + 3\alpha^2) p_0^2, \quad [\text{S7}]$$

which leads to $p = C_2 / u = p_0 \sqrt{(u^2 + 3/2\alpha^2) / (u + \alpha \cos(T))}$. The levitation pressure is the overpressure averaged across one cycle or

$$p_a = \int_0^{2\pi} p - p_0 dT = p_0 \left(\sqrt{\frac{u^2 + \frac{3}{2\alpha^2}}{u^2 - \alpha^2}} - 1 \right) \quad [\text{S8}]$$

for $\alpha < u$. For small separation u , the latter is well-approximated by the first term of its Taylor series expansion:

$$p_a = \frac{5}{4} p_0 \frac{\alpha^2}{u^2}. \quad [\text{S9}]$$

Predictions from squeeze film theory are close to the prediction made by acoustic radiation pressure, which takes into account inertia. For a small gap, near-field acoustic pressure is $(1 + \gamma)/4 \rho c^2 \alpha^2 / u^2$, with $\gamma = 1.4$ the adiabatic index, ρ the air density, and $c = \sqrt{\gamma p_0 / \rho}$ the speed of sound in air. The acoustic radiation pressure predicts a force 50% smaller than squeeze film theory with large squeeze number. Zhao et al. (32) showed that, for small separation, the squeeze film theory is closer to the experimental. Conversely, as the levitation distance reaches a value for which the squeeze number $\sigma < 36$, near-field acoustic levitation theory is more accurate (31).

Steady-State Equilibrium and Friction. In steady state, the time-averaged pressing pressure p_s is balanced by the time-averaged reaction of the support p_r (Eq. S1) and the time-averaged acoustic pressure from the squeeze film (Eq. S9):

$$p_s - p_r = p_a \quad [\text{S10}]$$

and

$$p_s \left[1 - \exp\left(\frac{(-u + u_0)}{u_{rms}}\right) \right] = \frac{5}{4} p_0 \frac{\alpha^2}{u^2}. \quad [\text{S11}]$$

Solving this equation leads to the interfacial separation u as a function of the amplitude of vibration- α . The main result is that the levitation distance is a monotonic function of the amplitude of vibration. The results of the model are presented in Fig. S3A and B. Indeed, as u increases, the exponential term approaches zero, and $u \rightarrow \sqrt{5p_0 / (4p_s)} \alpha$, which corresponds to the levitation distance that would result from the levitation of a smooth, rigid object (30).

Images of the contact and tribometry measurements both show a progressive decrease of contact area and friction force when the amplitude of vibration is increased. Larger interfacial separation will lead to fewer asperities in contact, therefore a reduced area of contact. Multiscale contact theory (16–18) notes that the true area of contact is proportional to the normal force, and therefore, we have the following relationship:

$$A = A_0 \exp\left(\frac{(-u + u_0)}{u_{rms}}\right), \quad [\text{S12}]$$

with A_0 the true area of contact in the absence of vibrations. The model is compared with tribometry measurement for each participant in Fig. S1. A study of the evolution of the interfacial separation and relative area of contact is presented in Fig. S3. When α is small, we have $u \approx u_0$ and $1 - \exp((-u + u_0)/u_{rms}) \approx (u - u_0)/u_{rms}$, which lead to the approximation of Eq. S11:

$$u - u_0 \approx \frac{5u_{rms} p_0}{4u_0^2 p_s} \alpha^2, \quad [\text{S13}]$$

and the true area of contact is closely approximated by a Gaussian centered at zero:

$$A \approx A_0 \exp\left(-\frac{\alpha^2}{2\Gamma}\right), \quad [\text{S14}]$$

with $\Gamma = 2u_0^2 p_s / (5 p_0)$ as the variance of the Gaussian function. Note that u_0 depends on the pressing force p_s and the nominal roughness height of the skin u_{rms} .

However, the variation of brightness and its nominal value shown in Fig. 4 can be found if we consider that the interfacial

separation is $\bar{u} = u + \alpha \sin(\omega t)$. Using this expression in S14, assuming $\alpha \ll u$, and using error propagation analysis, we find the rms of the variation to be

$$\frac{\Delta A}{A} = \frac{\alpha}{u_{rms}\sqrt{2}}. \quad [\text{S15}]$$

This relationship is shown as the regression line in Fig. 4E. The data depart from this ideal model probably because of the bouncing behavior and other phenomena that are not captured.

Contact Dynamics. Because the microsecond stroboscopy did not reveal any strong nonlinearities, it is fair to study the dynamics of the contact using linear time-invariant theory to the extent that the vibration amplitude remains small compared with the gap. At the range of frequencies used in this class of devices, the squeeze number is estimated to have a value higher than 300, which indicates that the film of air behaves elastically and that the dissipation induced by the airflow at the edge of the contact is small (38, 39).

The dynamic behavior of the skin can be modeled by a mass-spring-damper (m , k_t , and b_t) that captures the density and viscoelasticity of the tissues as well as other dissipation mechanisms. In this model, the squeeze film is represented by a spring k_{sq} that connects the displacement of the vibrating plate, $x_1 = \alpha \sin \omega t$, to the displacement of the mass, x_2 . The force f applied by the spring to the mass is proportional to the instantaneous gap $u = x_2 - x_1$. The equations of motion expressed in the Fourier domain are

$$\hat{f} = (k_t - m\omega^2 + ib_t\omega) \hat{x}_2 = \mathbf{T}(i\omega) \hat{x}_2 \quad [\text{S16}]$$

and

$$\hat{f} = -k_{sq} (\hat{x}_2 - \hat{x}_1) = \mathbf{S}(i\omega) (\hat{x}_2 - \hat{x}_1), \quad [\text{S17}]$$

with $i = \sqrt{-1}$. The previous equations can be combined into

$$(k_t + k_{sq} - m\omega^2 + ib_t\omega) \hat{x}_2 = k_{sq} \hat{x}_1 \quad [\text{S18}]$$

or

$$\frac{\hat{x}_2}{\hat{x}_1} = \frac{\mathbf{S}}{\mathbf{S} + \mathbf{T}}. \quad [\text{S19}]$$

The gap dynamics can be found by noting that $u = x_2 - x_1$:

$$\frac{\hat{u}}{\hat{x}_1} = -\frac{\mathbf{T}}{\mathbf{S} + \mathbf{T}}. \quad [\text{S20}]$$

Measurement of the impedance at ultrasonic frequencies shows that the finger is contributing a mass of $m = 0.5$ g, a damping of $b_t = 20$ N·s/m, and a stiffness in the order of $k_t = 10^3$ N/m (41). This model predicts that a phase of $220^\circ \pm 20^\circ$ between the motion of the plate and the motion of the skin is achieved when the squeeze film contributes a stiffness of $k_{sq} = 11 \pm 3 \times 10^6$ N/m, which is significantly higher than the stiffness of skin. This result is surprisingly robust to errors in evaluation of the damping, because less than 10% variation is observed for damping of the skin lower than $b_t = 70$ N·s/m. Fig. S4 shows the evolution of the amplitude and phase of the gap with respect to the excitation as well as the effect of varying the dynamic parameters of the linear time-invariant model.

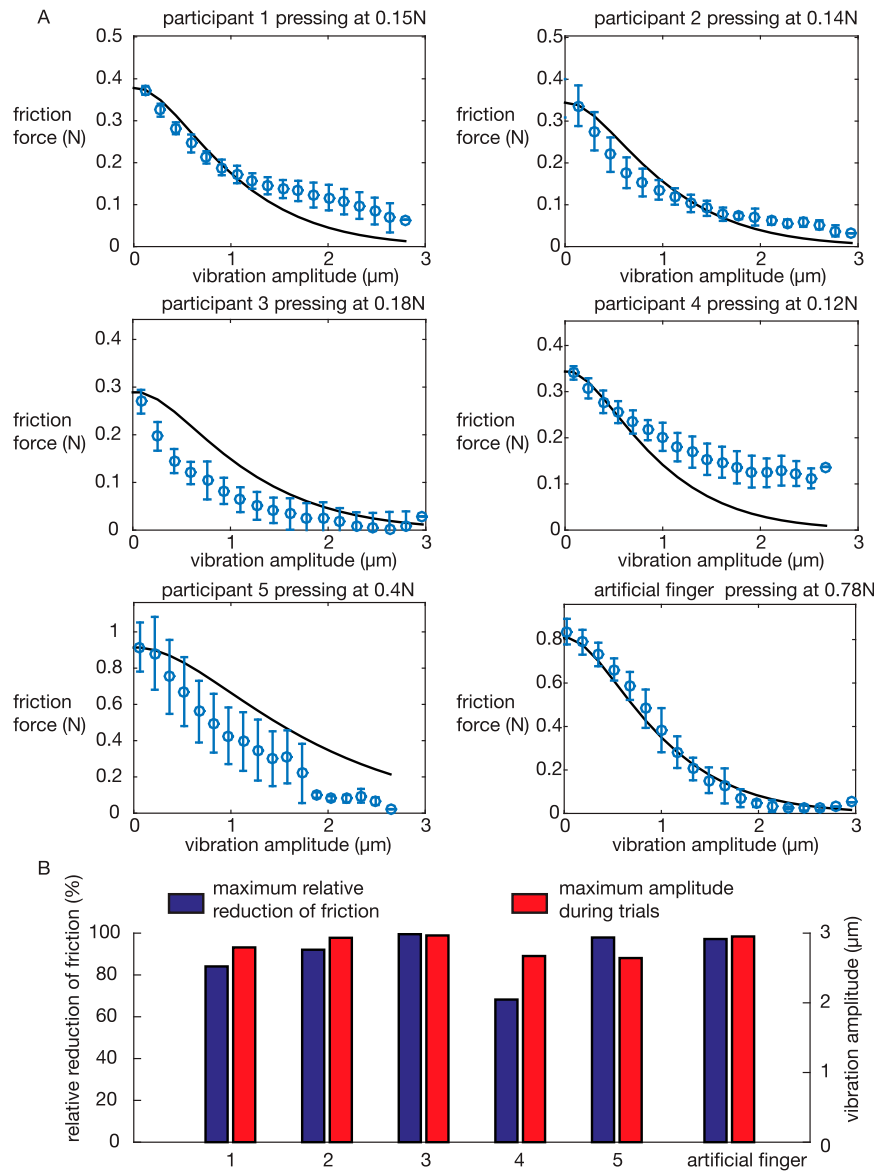


Fig. S1. (A) Friction measurement for each participant compared with the prediction from the model, with $u_{rms} = 5 \mu\text{m}$. (B) Summary of the effectiveness of the friction reduction at the maximum vibration amplitude tested.

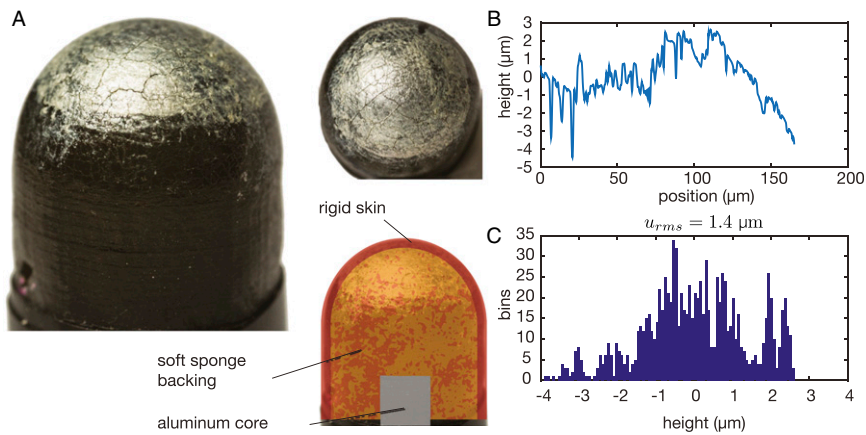
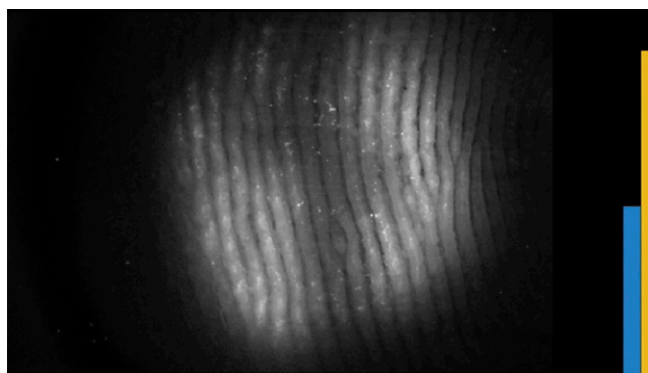


Fig. S6. (A) Picture of the artificial finger used in the study. (B) Results of interferometric measurement of the surface roughness. (C) Histogram of the surface profile.



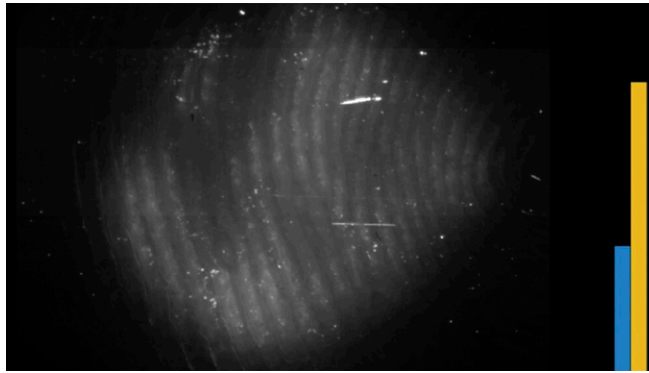
Movie S1. Effect of the modulation of friction on the finger dynamic during exploration. The green LED on the right indicates that the ultrasonic vibration is turned on. The high-amplitude vibration creates a drastic reduction of the coefficient of friction that facilitates finger motion.

[Movie S1](#)



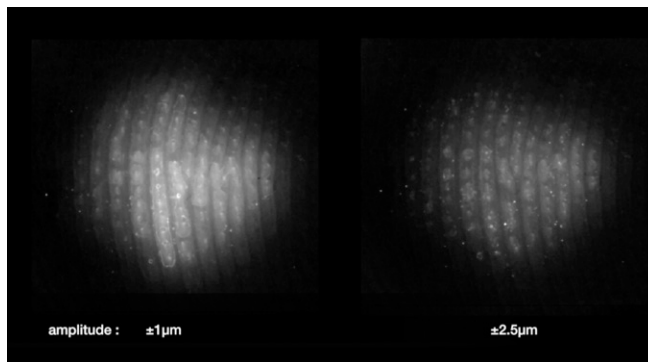
Movie S2. Long-exposure image of the contact during sliding. The blue bar shows the friction force experienced by the finger as it slides onto the glass plate. The yellow bar represents the amplitude of vibration. The envelope of the vibration follows a sine wave with a 1-s period. The increase in wave amplitude is linked to a reduction of the brightness of the contact and the frictional force.

[Movie S2](#)



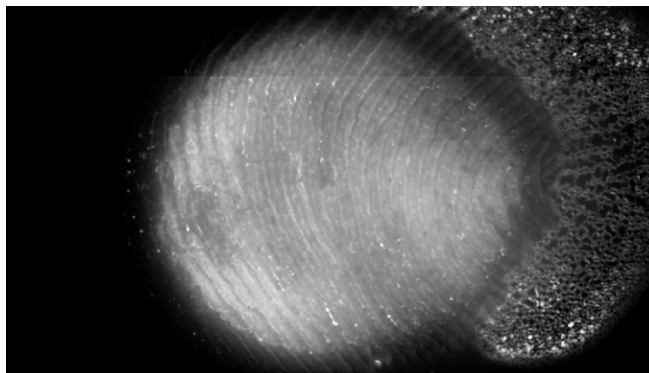
Movie S3. Long-exposure image of the contact during stimulation with a square waveform envelope. The sudden change in ultrasonic vibration amplitude leads to a progressive modification of the interfacial friction.

[Movie S3](#)



Movie S4. Stroboscopic contact imaging with a microsecond resolution. The brightness of the contact, which relates to the real area of contact, evolves during one cycle of the oscillation. The variation of brightness during one cycle is correlated with the amplitude of vibration.

[Movie S4](#)



Movie S5. A squeeze film air bubble breaks the adhesion from moisture.

[Movie S5](#)